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## Physics and Chemistry of Liquids

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# Study of the molecular interactions, excess molar volumes and viscosity deviations of ternary systems of 1-butanol (1) + 2-butanol (2) + 1,2butanediol (3) at 303.15 K

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### Study of the molecular interactions, excess molar volumes and viscosity deviations of ternary systems of 1-butanol (1)+2-butanol (2)+1,2-butanediol (3) at 303.15 K

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This article reports experimental densities and viscosities of ternary systems of 1-butanol (1) + 2-butanol (2) + 1,2-butanediol (3) and the binary systems of 1-butanol (1) + 2-butanol (2), 1-butanol (1) + 1,2-butanediol (3), and 2-butanol (2) + 1,2-butanediol (3), over the entire range of composition at 303.15 K. Excess molar volume  $V_{123}^E$ , viscosity deviations  $\Delta\eta_{123}$  for viscous flow were evaluated from the experimental data obtained. These derived properties for binary and ternary systems were fitted to Redlich–Kister and Cibulka's equations, respectively. The  $V_{123}^E$  data and  $\Delta\eta_{123}$  values were negative over the whole range of composition. Several semi-empirical relations are used to predict the binary and ternary viscosities and excess molar volume, and viscosity deviations from experimental results on the constituted ternaries and analysed to discuss the nature and strength of intermolecular interactions in these mixtures.

**Keywords:** excess molar volume; viscosity deviations; ternary system; 1-butanol; 2-butanol; 1,2-butanediol

#### 1. Introduction

Thermodynamic and transport property data are of great interest in process design and operation. Viscosity and density, vapour–liquid equilibrium data are required in many chemical engineering calculations involving fluid flow, heat and mass transfer. Moreover, knowledge of the dependence of viscosity and density on mixture composition is of considerable interest in understanding the intermolecular interactions [1–5]. This article, as part of a continuing study in our laboratory [6–10], reports the precise measurement of density and kinematic viscosity for the ternaries system formed by ternary system 1-butanol (1)+2-butanol (2) +1,2-butanediol, and constituted binary mixtures. Excess molar volumes and deviation in viscosities were calculated for the studied ternary mixtures on the excess properties because of their importance for inferring which type of interactions predominates in liquid mixtures.

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#### 2. Experimental section

#### 2.1. Materials

The mole fraction purity of the molecules from Merck were: 1-butanol ( $\geq 99\%$ ), 2-butanol ( $\geq 99\%$ ) and 1,2-butanediol ( $\geq 99\%$ ). Densities of the pure liquids and their mixtures at 303.15 K were measured with an Anton Paar digital densimeter (Model DMA 4500) operated in the static mode and capable of a precision of better than  $\pm 10^{-2}$  kg m<sup>-3</sup> and automatically thermostated within  $\pm 0.01$  K. Densities and viscosities of the pure reagents were in good agreement with values found in the literature [11–13], reported in Table 1.

#### 2.2. Apparatus and procedure

Viscosities at 303.15 K were measured with an Ubbleohde viscometer. The equation for viscosity is

$$\eta = \rho = \nu = \rho(kt - c/t),\tag{1}$$

where k and c are the viscometer constants and t,  $\eta$  and v are the efflux time, dynamic viscosity and kinematic viscosity, respectively. The dynamic viscosity was reproducible to within  $\pm 2 \times 10^{-3}$  mPa.s. The viscometer was suspended in a thermostated water bath maintained at  $\pm 0.01$  K.

#### 3. Results and discussion

#### 3.1. Binary systems

In Table 2, we show values of densities, dynamic viscosities for binary systems as well as the molar excess volume,  $V^E$  and viscosity deviations and  $\Delta \eta$  computed with the following equations.

$$V^{E}/(\text{cm}^{3}\text{mol}^{-1}) = \frac{\sum_{i=1}^{c} x_{i}M_{i}}{\rho} - \sum_{i=1}^{c} x_{i}\frac{M_{i}}{\rho_{i}}$$
(2)

$$\Delta \eta / (\text{mPa s}) = \eta - \sum_{i=1}^{c} x_i \eta_i, \qquad (3)$$

which are valid for ternary systems, as well. In the above equations the presence of the subindex *i* refer to the property of the pure component and the quantities without

|  | ho (kg                     | $gm^{-3}$ )   | п                          | рD  |
|--|----------------------------|---|----------------------------|---|
| Substance                                | Observed                   | Literature  | Observed                   | Literature  |
| 1-butanol<br>2-butanol<br>1,2 butanediol | 806.13<br>802.46<br>998.74 | 805.75 <sup>a</sup><br>802.72 <sup>b</sup><br>998.41 <sup>c</sup> | 1.3974<br>1.3950<br>1.4381 | 1.3973 <sup>a</sup><br>1.3953 <sup>a</sup><br>1.4381 <sup>a</sup> |

Table 1. Properties of the pure components at 303.15 K.

Note: <sup>a</sup>Reference [11]; <sup>b</sup>Reference [12]; <sup>c</sup>Reference [13].

| x             | $(\text{kg m}^{-3})$ | $\Delta \eta$ (mPa s) | $(\text{cm}^3 \text{mol}^{-1})$ | $\frac{\Delta\eta}{(\text{mPa s})}$ |
|---------------|----------------------|-----------------------|---------------------------------|-------------------------------------|
| x 1-butanol-  | +(1-x) 2-butanol     |                       |                                 |                                     |
| 0.050         | 798.53               | 2.401                 | -0.007                          | -0.011                              |
| 0.100         | 798.80               | 2.380                 | -0.015                          | -0.018                              |
| 0.149         | 799.07               | 2.361                 | -0.024                          | -0.025                              |
| 0.201         | 799.35               | 2.342                 | -0.032                          | -0.030                              |
| 0.248         | 799.59               | 2.326                 | -0.038                          | -0.033                              |
| 0.302         | 799.86               | 2.309                 | -0.045                          | -0.036                              |
| 0.353         | 800.10               | 2.294                 | -0.049                          | -0.037                              |
| 0.387         | 800.25               | 2.284                 | -0.050                          | -0.038                              |
| 0.449         | 800.51               | 2.267                 | -0.052                          | -0.039                              |
| 0.519         | 800.80               | 2.248                 | -0.052                          | -0.039                              |
| 0.550         | 800.92               | 2.240                 | -0.052                          | -0.039                              |
| 0.600         | 801.11               | 2.227                 | -0.051                          | -0.039                              |
| 0.650         | 801.28               | 2.215                 | -0.047                          | -0.038                              |
| 0.700         | 801.44               | 2.203                 | -0.043                          | -0.037                              |
| 0.750         | 801.60               | 2.192                 | -0.038                          | -0.034                              |
| 0.800         | 801.75               | 2.181                 | -0.032                          | -0.032                              |
| 0.851         | 801.89               | 2.173                 | -0.024                          | -0.027                              |
| 0.899         | 802.02               | 2.167                 | -0.017                          | -0.020                              |
| x 1-butanol - | +(1-x)1.2-butanedic  | ol                    |                                 |                                     |
| 0.050         | 985.80               | 26.032                | -0.047                          | -2.580                              |
| 0.101         | 976.08               | 22.947                | -0.077                          | -4.240                              |
| 0.150         | 966.63               | 20.158                | -0.097                          | -5.654                              |
| 0.200         | 957.08               | 17.424                | -0.114                          | -7.005                              |
| 0.297         | 938.42               | 13.138                | -0.131                          | -8.600                              |
| 0.350         | 928.12               | 11.031                | -0.136                          | -9.226                              |
| 0.400         | 918.31               | 9.519                 | -0.139                          | -9.326                              |
| 0.450         | 908.76               | 8.158                 | -0.141                          | -9.311                              |
| 0.500         | 899.18               | 7.134                 | -0.143                          | -8.953                              |
| 0.550         | 889.49               | 6.135                 | -0.143                          | -8.553                              |
| 0.600         | 879.85               | 5.321                 | -0.140                          | -7.977                              |
| 0.650         | 870.10               | 4.675                 | -0.136                          | -7.215                              |
| 0.699         | 860.66               | 4.120                 | -0.132                          | -6.407                              |
| 0.750         | 850.92               | 3.650                 | -0.123                          | -5.472                              |
| 0.799         | 841.32               | 3.236                 | -0.108                          | -4.507                              |
| 0.849         | 831.62               | 2.976                 | -0.088                          | -3.376                              |
| 0.900         | 821.77               | 2.589                 | -0.061                          | -2.356                              |
| x 2-butanol - | +(1-x)1.2-butanedic  | ol                    |                                 |                                     |
| 0.0499        | 985.43               | 26.560                | -0.041                          | -1.196                              |
| 0.0998        | 975.70               | 24.122                | -0.070                          | -2.302                              |
| 0.1499        | 965.84               | 21.521                | -0.089                          | -3.567                              |
| 0.1992        | 956.14               | 19.126                | -0.103                          | -4.650                              |
| 0.3009        | 936.04               | 14.224                | -0.121                          | -6.840                              |
| 0.3481        | 926.70               | 12.353                | -0.127                          | -7.451                              |
| 0.3995        | 916.55               | 10.631                | -0.129                          | -7.805                              |
| 0.4504        | 906.49               | 9.153                 | -0.131                          | -7.925                              |
| 0.5014        | 896.45               | 7.808                 | -0.133                          | -7 910                              |
| 0.5503        | 886.81               | 6.738                 | -0.131                          | -7.676                              |
| 0.5995        | 877.14               | 5.882                 | -0.129                          | _7 222                              |
| 0.6504        | 867.14               | 5.249                 | -0.126                          | -6.497                              |

Table 2. Excess molar volume and viscosity deviations of binary mixtures at 303.15 K.

(continued)

| x      | $(\text{kg m}^{-3})$ | $\frac{\Delta\eta}{(\text{mPa s})}$ | $(\text{cm}^3 \text{mol}^{-1})$ | $\Delta \eta$ (mPa s) |
|--------|----------------------|-------------------------------------|---------------------------------|-----------------------|
| 0.6994 | 857.51               | 4.641                               | -0.121                          | -5.797                |
| 0.7497 | 847.62               | 4.096                               | -0.110                          | -5.003                |
| 0.7999 | 837.75               | 3.635                               | -0.098                          | -4.125                |
| 0.8500 | 827.89               | 3.230                               | -0.082                          | -3.193                |
| 0.8994 | 818.16               | 2.928                               | -0.060                          | -2.180                |
| 0.9500 | 808.18               | 2.664                               | -0.034                          | -1.094                |

Table 2. Continued.



Figure 1. Excess molar volumes of the binary mixtures versus mole fraction x. Experimental results: ( $\blacklozenge$ ) x 1-butanol + (1 - x) 2-butanol, ( $\blacksquare$ ) x 1-butanol + (1 - x) 1,2 butanediol, ( $\blacktriangledown$ ) x 2-butanol + (1 - x) 1,2 butanediol. Redlich-Kister fit curves (—) at 303.15 K.

subindex refers to the property of the mixture. M is the molecular weight, x the mole fraction and c refers to the number of components in the mixture.

Figures 1 and 2 show the variation with composition of  $V^E$  and  $\Delta \eta$  for the binary systems [(x) 1-butanol + (1 - x) 2-butanol, + (1 - x) 1,2-butanediol and (x) 2-butanol + (1 - x) 1,2-butanediol]. As seen in Figure 1 and Table 2, the measured  $V^E$  are negative over the entire range of mole fractions for the binary systems. The values of  $\Delta \eta$  (Figure 2) were negative over the whole composition range for all of the binary systems studied herein. The sign of  $\Delta \eta$  is in agreement with the conclusion by Fort and Moore [14] who proposed that the negative values of this property are characteristic of systems where dispersion forces are predominate.

The  $V^E$  and  $\Delta \eta$  values were correlated with composition, using the Redlich-Kister equation [15].

$$Y = x(1-x)\sum_{i=0}^{p} A_i(2x-1)^i,$$
(4)



Figure 2. Excess dynamic viscosity of the binary mixtures versus mole fraction x. Experimental results: ( $\blacklozenge$ ) x 1-butanol+(1-x) 2-butanol, ( $\blacksquare$ ) x 1-butanol+(1-x) 1,2 butanediol, ( $\blacksquare$ ) x 2-butanol+(1-x) 1,2 butanediol. Redlich-Kister fit curves (—) at 303.15 K.

Table 3. Values of adjustable coefficient,  $A_k$  in Equation (4) and standard deviation,  $\sigma$  in Equation (5) for excess molar values and viscosity deviation for binary mixtures at 303.15 K.

|   | $A_0$         | $A_1$   | $A_2$   | $A_3$   | $A_4$    | σ      |
|---|---------------|---------|---------|---------|----------|--------|
| x 1-butanol $+(1 -$                     | x) 2-butanol  |         |         |         |          |        |
| $V^E (\text{cm}^3 \text{mol}^{-1})$     | -0.2105       | 0.0129  | 0.0111  | -0.0334 | 0.0639   | 0.0004 |
| $\Delta \eta$ (mPa s)                   | -0.1572       | -0.0101 | -0.0862 | 0.0022  | -0.0126  | 0.0004 |
| x 1-butanol + $(1 - $                   | x) 1,2-butane | ediol   |         |         |          |        |
| $V^E (\text{cm}^3 \text{mol}^{-1})$     | -0.5721       | -0.0662 | -0.3199 | 0.2784  |          | 0.0017 |
| $\Delta \eta$ (mPa s)                   | -36.5310      | 12.3210 | 10.3700 | 2.3402  | -18.8070 | 0.1425 |
| x 2-butanol $+(1 -$                     | x) 1,2-butane | ediol   |         |         |          |        |
| $V^E (\mathrm{cm}^3 \mathrm{mol}^{-1})$ | -0.5244       | -0.0080 | -0.3151 | 0.1133  |          | 0.0012 |
| $\Delta \eta$ (mPa s)                   | -31.7970      | 5.8739  | 13.2630 | -6.5819 | -4.4821  | 0.0784 |

where  $Y \equiv (V^E \text{ or } \Delta \eta)$  and x is the mole fraction of the first component. The coefficients  $A_i$  were calculated by the unweighted least-square method and the computed values and standard deviation for each of the properties are shown in Table 3.

In each case, the optimum number of coefficients was ascertained from an examination of the variation of standard deviations,  $\sigma$  with

$$\sigma = \left[\frac{\sum \left(Y_{\text{exp.}} - Y_{\text{cal.}}\right)^2}{(n-p)}\right]^{1/2},\tag{5}$$

where  $Y_{exp}$  and  $Y_{cal}$  are the experimental and calculated values of the property Y, respectively, and n and p are the number of experimental points and number of parameters retained in the respective equations. The standard deviations,  $\sigma$ , are also shown in Table 3.

#### 3.2. Ternary systems

The results for densities and excess molar volumes and viscosity deviations for the above ternary systems are reported in Table 4.

The excess molar volumes and viscosity deviations were correlated with ternary composition using the equation proposed by Cibulka [16].

$$Y_{123} = Y_{\text{bin}} + x_1 x_2 (1 - x_1 - x_2) (B_0 + B_1 x_1 + B_2 x_2)$$
(6)

where  $Y \equiv (V^E \text{ or } \Delta \eta)$  and  $Y_{\text{bin}} = Y_{12} + Y_{13} + Y_{23}$  are the so called 'binary contribution'.

Table 4. Excess molar volume and viscosity deviations of ternary mixtures 1-butanol (1) + 2-butanol (2) + 1, 2 butandiol (3) at 303.15 K.

| <i>X</i> <sub>1</sub> | <i>X</i> <sub>2</sub> | $\rho$ (kg m <sup>-3</sup> ) | $\Delta \eta$ (mPa s) | $V^E$ (cm <sup>3</sup> mol <sup>-1</sup> ) | $\Delta \eta$<br>(mPa s) |
|-----------------------|-----------------------|------------------------------|-----------------------|--|--------------------------|
| 0.100                 | 0.099                 | 955.87                       | 18.089                | -0.036                                     | -5.657                   |
| 0.098                 | 0.201                 | 936.20                       | 13.991                | -0.041                                     | -7.096                   |
| 0.098                 | 0.301                 | 916.16                       | 10.182                | -0.040                                     | -8.239                   |
| 0.100                 | 0.400                 | 896.10                       | 7.054                 | -0.017                                     | -8.686                   |
| 0.100                 | 0.499                 | 876.75                       | 4.820                 | -0.033                                     | -8.272                   |
| 0.100                 | 0.599                 | 857.11                       | 3.348                 | -0.031                                     | -7.069                   |
| 0.100                 | 0.699                 | 838.30                       | 2.540                 | -0.010                                     | -5.213                   |
| 0.100                 | 0.799                 | 818.13                       | 2.214                 | -0.013                                     | -2.868                   |
| 0.200                 | 0.099                 | 936.96                       | 13.379                | -0.085                                     | -7.686                   |
| 0.202                 | 0.199                 | 916.10                       | 9.684                 | -0.035                                     | -8.647                   |
| 0.200                 | 0.300                 | 896.45                       | 6.545                 | -0.012                                     | -9.164                   |
| 0.202                 | 0.399                 | 876.71                       | 4.041                 | -0.019                                     | -8.981                   |
| 0.200                 | 0.500                 | 857.22                       | 2.447                 | -0.007                                     | -7.933                   |
| 0.198                 | 0.602                 | 837.85                       | 1.680                 | -0.020                                     | -6.030                   |
| 0.206                 | 0.694                 | 818.55                       | 1.607                 | -0.028                                     | -3.431                   |
| 0.298                 | 0.103                 | 916.87                       | 9.405                 | -0.038                                     | -8.943                   |
| 0.299                 | 0.201                 | 897.15                       | 6.304                 | -0.027                                     | -9.397                   |
| 0.299                 | 0.301                 | 877.44                       | 3.704                 | -0.028                                     | -9.329                   |
| 0.300                 | 0.400                 | 857.86                       | 1.924                 | -0.027                                     | -8.436                   |
| 0.298                 | 0.501                 | 838.28                       | 1.102                 | -0.006                                     | -6.606                   |
| 0.300                 | 0.600                 | 819.52                       | 1.204                 | -0.081                                     | -3.827                   |
| 0.397                 | 0.104                 | 897.47                       | 6.249                 | -0.037                                     | -9.401                   |
| 0.398                 | 0.202                 | 877.93                       | 3.689                 | -0.032                                     | -9.319                   |
| 0.400                 | 0.299                 | 858.41                       | 1.798                 | -0.025                                     | -8.558                   |
| 0.400                 | 0.400                 | 839.20                       | 0.836                 | -0.077                                     | -6.827                   |
| 0.402                 | 0.498                 | 819.26                       | 0.971                 | -0.016                                     | -4.025                   |
| 0.502                 | 0.099                 | 878.26                       | 4.084                 | -0.031                                     | -8.884                   |
| 0.500                 | 0.200                 | 858.58                       | 2.077                 | -0.019                                     | -8.230                   |
| 0.500                 | 0.300                 | 839.28                       | 0.924                 | -0.040                                     | -6.716                   |
| 0.500                 | 0.400                 | 819.68                       | 0.880                 | -0.013                                     | -4.100                   |
| 0.599                 | 0.101                 | 859.03                       | 2.784                 | -0.018                                     | -7.503                   |
| 0.600                 | 0.200                 | 839.66                       | 1.373                 | -0.012                                     | -6.263                   |
| 0.600                 | 0.300                 | 820.07                       | 1.069                 | -0.010                                     | -3.887                   |
| 0.700                 | 0.100                 | 839.96                       | 2.134                 | -0.023                                     | -5.458                   |
| 0.700                 | 0.199                 | 820.83                       | 1.397                 | -0.020                                     | -3.572                   |
| 0.799                 | 0.104                 | 820.43                       | 1.882                 | -0.020                                     | -2.955                   |

The coefficients,  $B_p$  and standard deviations,  $\sigma$  (Equation (5)) obtained by the least-squares method are given in Table 5.

#### 4. Prediction of viscosity of binary and ternary systems

Several semi-empirical relations have been proposed to estimate the viscosity of liquid mixtures in terms of pure component data. We have examined the following equations for binary system:

(1) The single-parameter Grunberg-Nissan [17] equation is

$$\eta = \exp(x_1 \ln \eta_1 + x_2 \ln \eta_2 + x_1 x_2 G_{12}), \tag{7}$$

where  $G_{12}$  is a parameter proportional to the interchange energy.

(2) Hind et al. [18] proposed the following equation:

$$\eta = x_1^2 \eta_1 + x_2^2 \eta_2 + 2x_1 x_2 \eta_{12},\tag{8}$$

where  $\eta_{12}$  is attributed to unlike pair interactions.

(3) The two-parameter McAllister [19] equation based on Eyring's theory of absolute reaction rates and three-body interaction model is

$$\ln v = x_1^3 \ln v_1 + 3x_1^2 x_2 \ln Z_{12} + 3x_1 x_2^2 \ln Z_{21} + x_2^3 \ln v_2 - \ln(x_1 + x_2 M_2/M_1) + 3x_1^2 x_2 \ln(2/3 + M_2/3M_1) + 3x_1 x_2^2 \ln(1/3 + 2M_2/3M_1) + x_2^3 \ln(M_2/M_1),$$
(9)

where  $Z_{12}$  and  $Z_{21}$  are interaction parameters and  $M_i$  and  $v_i$  are the molecular mass and kinematics' viscosity of pure component *i*, respectively.

(4) The no-parameter equation of Kendall and Monroe [20] is expressed as

$$\eta = (x_1 \eta_1^{1/3} + x_2 \eta_2^{1/3})^3.$$
<sup>(10)</sup>

(5) The Frenkel equation [21]:

$$\eta = x_1^2 \eta_1 + x_2^2 \eta_2. \tag{11}$$

In ternary system the result is fitted by Grunberg-Nissan and Frenkel's equations. The correlating ability of each of Equations (8)-(11) was tested and

Table 5. Fitting parameters for Cibulka equation and standard deviations,  $\sigma$ , for excess molar volume and viscosity the ternary system at T = 303.15 K.

|                                   | $B_0$          | $B_1$       | $B_2$     | σ      |
|-----------------------------------|----------------|-------------|-----------|--------|
| 1-butanol (1) + 2-but             | (2) + 1,2-buta | inediol (3) | 2 0 101   | 0.00(1 |
| $V^2 (\text{cm}^2 \text{ mol}^2)$ | 5.9922         | -3.164/     | -3.9491   | 0.0264 |
| $\Delta \eta \ (mPa s)$           | 56.8258        | -143.0790   | -132.0460 | 0.0090 |

|                            | x  1-butanol + (1 - x)<br>2-butanol        | x 1-butanol + $(1 - x)$<br>1,2-butanediol | x 2-butanol + $(1 - x)$<br>1,2-butanediol |
|----------------------------|--|---|---|
| Grunberg a                 | nd Nissan                                  |   |   |
| G <sub>12</sub>            | -0.0340                                    | 0.8106                                    | -0.1091                                   |
| σ                          | 0.0031                                     | 0.4421                                    | 0.9421                                    |
| Kendall and                | l Monroe                                   |   |   |
| σ                          | 0.0326                                     | 0.9543                                    | 0.1501                                    |
| Frenkel                    |  |   |   |
| σ                          | 0.0031                                     | 0.7701                                    | 0.9421                                    |
| Hind et al.                |  |   |   |
| $\eta_{12}$                | 2.2075                                     | -1.1136                                   | 0.4754                                    |
| σ                          | 0.0030                                     | 0.2080                                    | 0.2260                                    |
| McAllister t               | hree-body                                  |   |   |
| $\ln(v_{12})$              | 1.0039                                     | 1.4758                                    | 1.5475                                    |
| $\ln(v_{21})$              | 1.0473                                     | 2.5910                                    | 2.8439                                    |
| σ                          | 0.0003                                     | 0.1434                                    | 0.2329                                    |
| 1-butanol (1<br>Grunberg a | ) + 2-butanol (2) + 1,2-butan<br>nd Nissan | nediol(3)                                 |   |
| G122                       | ind i tibbuli                              | -7.6957                                   |   |
| $\sigma$                   |  | 0.6505                                    |   |
| Ferenkel                   |  |   |   |
| $\ln(A_{122})$             |  | 3.4211                                    |   |
| σ                          |  | 0.8305                                    |   |
|                            |  |   |   |

| Table 6.  | Adjustable     | parameters | of | Equations | (7)-(11) | and | standard | deviations | of | binary |
|-----------|----------------|------------|----|-----------|----------|-----|----------|------------|----|--------|
| mixture v | viscosities at | 303.15 K.  |    |           |          |     |          |            |    |        |

Table 7. Standard deviations,  $\sigma$ , in the predictions,  $V_{123}^E$  (cm<sup>3</sup>mol<sup>-1</sup>) and  $\Delta \eta_{123}$  (mPa s), with different models for the ternary system at T = 303.15 K.

|                             | $\sigma (V_{123}^E)$ | $\sigma (\Delta \eta_{123})$ |
|-----------------------------|----------------------|------------------------------|
| Radojkovic                  | 0.0826               | 0.5868                       |
| Rastogi                     | 0.0822               | 0.9643                       |
| Kohler                      | 0.0444               | 0.9084                       |
| Jacob and Fitzner           | 0.0878               | 0.9845                       |
| Tsao and Smith <sup>a</sup> | 0.1660               | 0.7254                       |
| Tsao and Smith <sup>b</sup> | 0.2003               | 0.7074                       |
| Tsao and Smith <sup>c</sup> | 0.0783               | 0.6522                       |
| Colinet                     | 0.1517               | 0.6558                       |
| Toop <sup>a</sup>           | 0.1755               | 0.6296                       |
| Toop <sup>b</sup>           | 0.0989               | 0.6069                       |
| Toop <sup>c</sup>           | 0.1820               | 0.7361                       |
| Scatchard <sup>a</sup>      | 0.2183               | 0.6224                       |
| Scatchard <sup>b</sup>      | 0.0453               | 0.6165                       |
| Scatchard <sup>c</sup>      | 0.0628               | 0.4485                       |

their adjustable parameters and standard deviations ( $\sigma$ ):

$$\sigma = \left[\frac{1}{n-k}\sum\left\{\frac{(\eta_{\exp} - \eta_{cal})}{\eta_{\exp}}\right\}^2\right]^{1/2},\tag{12}$$

where n represents the number of data points and k is the number of numerical coefficients are given in Table 6. The results show that the two-parameter McAllister equation is the best for calculating the correlation of viscosity of binary mixtures.

Although prediction of the physical properties of multicomponent mixtures from those of their pure components is generally unreliable because of mixing effects, numerous schemes have been put forward for predictions based on the properties of the binary systems formed by pairs of components of the multicomponent system. In this work we applied the following models: Tsao–Smith [22], Jacob–Fitzner [23], Kohler [24], Rastogi et al. [25], Radojkovic et al. [26], Colinet [27], Toop [28] and Scatchard et al. [29]. Standard deviations,  $\sigma$ , presented in Table 7 were determined for all models with Equation (12). The standard deviations are obtained from the Kohler model for excess molar volume and from the Scatchard model for viscosity deviations of small values.

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